

SEMI-ACTIVE CONTROLLED BASE-ISOLATION SYSTEM WITH MAGNETORHEOLOGICAL DAMPER AND PENDULUM SYSTEM

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SUMMARY

As part of a large experimental testing program, the performance tests are conducted at NCREE on a 20 kN magnetorheological (MR) damper. Modified Bouc-Wen models are used to represent the MR damper. System parameters in the modified Bouc-Wen models that represent behavior of the MR damper are determined through on-line identification from data obtained during the performance tests. Validations of these mathematical models are conducted and results are found to be good. Next, dynamic performance of a 12-ton mass that is base-isolated by a pendulum system at each corner is investigated. This isolation system is tested on a shake table. Then, the 20 kN MR damper is rigidly connected to the mass and the shake table. The hybrid base-isolation system is controlled in a passive mode using different levels of constant current to the MR damper during motion of the shake table. Finally, different semi-active algorithms are used to control resistance of the MR damper can effectively mitigate structural response (both displacement and acceleration responses) under strong earthquake excitations. Low power consumption, direct feedback, high reliability, and fail-safe operation are validated in this study. In summary, this semi-active control system with a large controllable MR damper shows promise for application in real civil engineering structures.

INTRODUCTION

While standard base isolation techniques such as insertion of rubber bearings between the ground and a structure that is to be protected have been applied for a number of years Naeim [1], the addition of supplemental damping devices is being considered for large structures in order to create more robust resistance to a variety of earthquake characteristics. One recent comprehensive study Chang [2] used experimental and analytical methods to determine effectiveness of using lead-rubber or sliding bearings along with friction and viscous dampers for isolation of rigid structures. Supplemental passive damping devices have been found to be effective in reducing both displacement and base shear for structures that have moderately long periods.

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Other researchers are studying the ability of semi-active devices to reduce vibrations in structures. Very small power consumption, high reliability and a fail-safe mechanism make semi-active control one of the more promising approaches for the mitigation of damage due to seismic events in civil engineering structures. There are fundamentally two types of semi-active control devices. The first type uses a mechanical system to alter behavior of the control device; examples of such systems include the variable damping device, for example Sadek [3] and Symans [4], semi-active hydraulic damper, for example Kurata [5], Niwa [6] and a variable stiffness system, for example Kobori [7]. The basic approach is to use a variable valve to modify damping and stiffness of the damper. The second type of semi-active control device uses a controllable fluid, such as electrorheological (ER) , for example Burton [8] or magnetorheological (MR) fluid, for example Spencer [9] and Lin [10]. In this case an applied field that is electric or magnetic changes mechanical properties of the fluid and controls force in the damper.

The latter technique, which involves MR damper technology, is receiving a great deal of attention among researchers investigating control of large civil engineering structures. An MR damper resembles an ordinary linear viscous damper except that the cylinder of the damper is filled with a special fluid that contains very small polarizable particles. Viscosity of the fluid can be changed very quickly from a liquid to a semi-solid and vice versa. This is accomplished by adjusting the magnitude of the magnetic field produced by a coil wrapped around the piston head of the damper. When no current is supplied to the coil, an MR damper behaves in a manner that is similar to that of an ordinary viscous damper. On the other hand, when current is sent through the coil, fluid inside the damper becomes semi-solid and its yield strength depends on the applied current, for example Chang [11]. Since the control force is not applied directly to the structure by the damper, but rather only the resistance of the damper is adjusted, control instability does not occur and only a small amount of energy is required. Therefore, an MR damper is a reliable and fail-safe device.

This study makes use of a supplemental MR damper in a large structure that is equipped with the rolling pendulum system as the base-isolation system in a laboratory. The goal is to exploit the reliability and simplicity of a traditional base isolator with another reliable device that is able to change its characteristics within milliseconds. Rapid adjustment of a large MR damper to its surroundings allows the hybrid base-isolation system to provide safe and effective filtering of a broad range of motions from near- and far-fault seismic events.

In this study, the system identification of the 20 kN MR damper is carried out first, then the design of the semi-active control system with the Fuzzy logic control algorithm is presented. Next, the experimental setup of the semi-active controlled base-isolation system and test results of the shaking table test are illustrated. Finally, some conclusion come are made.

SYSTEM IDENTIFICATION

In order to use the 20kN MR damper to control a base-isolation system, it is necessary to study the physical behavior of the device as an independent subcomponent. To accomplish this task, a series performance tests are conducted on the damper at NCREE. Figure 1 shows the hysteresis loops and force/velocity relationships with different constant command voltage levels of one sinusoidal test. The MR damper shows a great variation with different command voltages. The wider controllable rang MR damper can increase the adjustable rang and also the control effect of the semi-active control system.

According to the force-displacement behaviors in the performance test, a modified Bouc-Wen model is used to represent the nonlinear response. And, the on-line identification algorithm is used to identify the model parameters. Equation 1 shows the identified model for the MR damper. In which, x represents relative displacement, \dot{x} represents relative velocity, and V is the command voltage. (Units: MN-m-sec-V.). The other performance test data, which is not used in the system identification, is used to validate the accuracy of the identified model for the MR damper. Figure 2 show one of the validation results. The red line represents the measured damper force, and the greed one represents the re-simulated damper force. According to the validation data, the identified Bouc-Wen model can represent the

nonlinear behavior of the MR damper well. (The detail identification procedure is shown in Lin [11].)

$$\begin{cases} F(t) = F_{d}(t) + z(t) \\ z(k) = z(k-1) + \sum_{i=1}^{5} \theta_{i}(k-1)\phi_{i}(k-1)dt \\ \Phi(k) = \Delta t * [\dot{x}(k), |\dot{x}(k)| | z(k)|^{0} z(k), \dot{x}(k) | z(k)|^{1}, |\dot{x}(k)| | z(k)|^{1} z(k), \dot{x}(k) | z(k)|^{2}]^{T} \\ \begin{cases} F_{d}(t) = 0.0083V(t) + 0.005 \\ \theta_{1} = -13.2924V^{3} + 22.9678V^{2} + 1.0297 V - 1.0762 \\ \theta_{2} = -161.6060V^{2} - 88.7154V - 389.2721 \\ \theta_{3} = -5.0428V^{2} - 169.2379V - 160.4490 \\ \theta_{4} = -6433V^{2} - 80282V - 7757 \\ \theta_{5} = 0.3452V^{2} - 6.775V - 0.316 \end{cases}$$
(1)



Figure 1: Hysteresis loops (left plot) and damper force/velocity relationships (right plot) of the 20 kN MR damper with different command voltage inputs in the sinusoidal test (1Hz / 40mm).



Figure 2: Comparison of the measured and re-simulated hysteresis loops of the MR damper in the validation test.

DESIGN OF SEMI-ACTIVE CONTROL

The semi-active control device used in this study is the 20 kN MR damper. Although its resistance to motion can be changed on command, it can not be treated like an active actuator for purposes of numerical simulation. Moreover, traditional active control algorithms cannot be directly applied to this

hybrid control system. Therefore, semi-active controllers are developed in the context of the nonlinear base-isolated structure with rolling pendulum system and MR damper subcomponents. Fuzzy logic is used to map an input space to an output space by means of if-then rules, see Fuzzy Logic Toolbox Users Guide [12]. Control components of the input signal are transformed into linguistic values through a fuzzification interface at each time step. Use of a fuzzy controller is advantageous in that performance is not overly sensitive to changes in the input signal. For output the mapped linguistic values are transformed into numerical values through a defuzzification interface.

Design of a fuzzy logic controller is separated into three parts: (1) use a fuzzy inference system (FIS) editor to define the number of input and output variables and choose the type of inference to be used; (2) define membership functions for the input and output variables; and (3) define if-then rules. In this study, a trial and error process results in the use of two inputs (displacement and acceleration) and one output (voltage) variable. Next, triangular membership functions and the range of their variables are defined for each input and output variable. Finally, the if-then rules are edited so as to connect each input and output

For the semi-active controller, S3, the absolute acceleration and relative displacement are selected as inputs, and the output is the command voltage. The number of membership functions used for the inputs are five and six, while seven membership function are used for the output. The first input, absolute acceleration, uses "PH", "PS", "Z", "NS" and "NH" the second input, relative displacement, uses "PH", "PB", "PS", "NS", "NB" and "NH" the output variable, force, uses "PH", "PB", "PS", "Z", "NS", "NB" and "NH". Figure 3 (a), (b) and (c) show the result of applying the inputs and output membership functions over the whole range of the input variables for semi-active control case "S3". Figure 3 (d) shows the control surface of semi-active control case "S3".

The design approach for semi-active control case "S3" is to control both the absolute acceleration and the relative displacement. As result, it divides the response of the isolation system into three kinds. First, when the absolute acceleration is huge, the command voltage is small when relative displacement is small and big when the relative displacement is huge. In this situation, the command voltage is suppressed to prevent exciting the acceleration responses except when the relative displacement is also huge. Secondly, when the absolute acceleration is small, the command voltage is increase with the relative displacement, and as huge as possible. In short word, the command voltage is as huge as possible except the small response zone. Thirdly, when the absolute acceleration is almost zero, the command voltage is zero when relative displacement is small and small when the relative displacement is big and huge. This part provides a zero command voltage belt around tiny acceleration responses. It can force the MR damper to be soft when the excitation is over.

SHAKING TABLE TESTS

Experimental setup

In this study, a base-isolated structure with rolling pendulum system and a 20 kN MR damper is tested on a shake table. Unlike the traditional isolators, such as high damping rubber bearing (HDRB), for example Lin [11] or friction pendulum bearing, for example Wang [13], the rolling pendulum system (RPS) is used in this study. The rolling pendulum system can provide the lowest resistance, and the adjustable MR damper can be the main energy absorber of the hybrid base-isolation system. As results, the controllable range of the semi-active control system can be maximized.

The goal of the shaking table test is to verify effectiveness of the hybrid control system with physical hardware and real-time processing requirements. Figure 4 shows a schematic drawing of the experimental setup. The shaking table controlled by the MTS system derives the desire earthquake excitation. The system responses are measured by the accelerometers, load cells, thermal couples and LVDTs, and send to the data acquisition system and some of them also feedback to the semi-active control system (PC/Simulink). Through the semi-active control surface (pre-loaded in PC/Simulink) and the feedback signals, the command voltage can be calculated online. The command voltage is converted to command current by VCCS and feed to the MR damper to optimal control the hybrid base-isolation

system.



Figure 3: Input and output membership functions of semi-active control surface "S3".

An array of LVDTs, accelerometers, load cells and a thermal couple are used to measure the displacement, absolute acceleration, force and temperature, respectively, at salient locations on the experimental structure. Figure 5 (a) shows the configuration of the experimental sensors. Displacements and accelerations of the base-isolated system are grouped into three levels: base of the rolling pendulum system (D0, A0), base of the isolated structure (D1, A1) and top of the isolated structure (D2, A2). Two LVDTs are placed at each level in order to measure both transverse and accidental torsional response. An additional LVDT is used to measure displacement response of the piston relative to the cylinder of the MR damper (Dmr). One additional accelerometer provides information concerning, the piston of the MR damper. A load cell (Lmr) is attached in-line with the axis of the MR damper in order to measure axial force. Finally, since temperature of the MR fluid is an important factor for reliable operation of the damper.

The isolated structure is constructed with a steel frame and lead blocks that provide the specified mass (12 and 24 tons). The natural period of the rolling pendulum system (As shown in Figure 5(b)) is selected as 2.77 sec. Ends of the 20 kN MR damper (as shown in Figure 5 (c)) are securely attached to the top surface of the shake table and the side of the isolated structure.

Time histories of recorded earthquakes are feed into a computer that controls the shake table. Due to

interaction between the table and test structure, a trial and error process of several iterations of the earthquake motion is used to compensate for the interaction so that a close approximation to the desired base motion is obtained.



Figure 4: Experimental setup of test structure.

A load cell (Lmr) is attached in-line with the axis of the MR damper in order to measure axial force. Finally, since temperature of the MR fluid is an important factor for reliable operation of the damper, one thermal couple (Tmr) is attached to the surface of the by-pass cylinder of the MR damper.

Time histories of recorded earthquakes are feed into a computer that controls the shake table. Due to interaction between the table and test structure, a trial and error process of several iterations of the earthquake motion is used to compensate for the interaction so that a close approximation to the desired base motion is obtained.



Figure 5: Configuration of the experimental sensors and photo of the 20 kN MR damper and rolling pendulum system.

Shaking table test cases

Figure 6 shows the photo of the 24-ton test structure in NCREE, 2003. Two different mass of the upper structure, two passive control case (minimum and maximum resistance) and three semi-active control cases are tested in the shaking table test. Table 1 shows the detail descriptions of the control cases made in the shaking table test. All the cases employ four rolling pendulum pads along with the 20 kN MR damper. The passive cases, termed "P-0V" and "P-0Vb", which use zero voltage, are used to simulate a failure situation in which the MR damper undergoes a loss of power. The passive cases, termed "P-1V" and "P-1Vb" which use one voltage are used to simulate the full power situation of the MR damper. The semi-active control cases, labeled "S1", "S2" and "S3" use feedbacks from sensors and different semi-active controllers (S1, S2 and S3) to adjust resistance of the MR damper. The limits of the input are used to confine the input signals to the identity rang with the semi-active controllers. In addition, the low pass filter is used to filter out the undesired high-frequency noise form the sensors.

Case	Mass	Control Type	Controller	Limits of Input	Low pass filter
P-0V	24	Passive/0V	Constant command Voltage 0Volt		
P-1V	24	Passive/1V	Constant command Voltage 1Volt		
S1	24	Semi-active	S1	Acc.: ±1 m/s ²	No
				Disp.: ±0.02 m	No
S2	24	Semi-active	S2	Acc.: $\pm 1(m/s^2)$	25 Hz
				Disp.: ±0.035(m)	50 Hz
P-0Vb	12	Passive/0V	Constant command Voltage 0Volt		
P-1Vb	12	Passive/1V	Constant command Voltage 1Volt		
S3	12	Semi-active	S3	Acc.: ±1(m/s ²)	25 Hz
				Disp.: ±0.035(m)	50 Hz

Table 1: Descriptions of the control cases made in the shake table test.

Excitation records that are investigated include El Centro, Kobe and Chi-Chi (at stations TCU052 and TCU068). Figure 7 shows the ground acceleration time histories and their fast Fourier transforms (FFTs) of the four earthquake records. Fast Fourier transforms (FFTs) of the time histories show that frequency content of the El Centro earthquake is relatively wide (0~8 Hz) while the near-fault Kobe earthquake has

significant low frequency components. Similarly, Chi-Chi earthquake accelerations are recorded very close to a fault, and the time history of ground acceleration includes a very low frequency wave. Peak ground acceleration (PGA) levels of 50, 100, 200, 300 and 400 gal are specified for the shaking table. The maximum PGA that is applied by the shaking table for each earthquake is limited by the 50 mm displacement capacity of the MR damper.



Figure 6: Photo of the Semi-active controlled base-isolation system composed with the rolling pendulum system and MR damper.

Shaking table test results

Effectiveness of each control scheme can be determined from data collected during testing on the shake table. Data are presented in the following discussion first according to maximum response and, second, using time-history response. As numerous sensors are used, tabulation of performance indices facilitates comparison of the control schemes. To this end, a set of indices is used to define maximum values of the following quantities: (1) stroke of the MR damper (Dmr), (2) relative displacement at the bottom of the isolated structure (D1), (3) relative displacement of the top of the isolated structure (D2), (4) input acceleration (A0), (5) absolute acceleration of the base of the isolated structure (A1), (6) absolute acceleration of the top of the isolated structure displacement. Relative displacements of the base and top of the isolated structure (D1 and D2) are the mean values of the measured responses from two LVDTs at each of the two levels. Indices 4-6 compare the degree of control of the maximum absolute acceleration. Absolute acceleration at the base and top of the isolated structure is also taken to be the mean value of the measured responses from two acceleration. Indices 4-7 compares maximum force supplied by the MR damper.

As the upper structure is very rigid, the most important control effect indices are relative displacement at the bottom of the isolated structure (D1) and absolute acceleration of the base of the isolated structure (A1). The stroke of the MR damper (Dmr) is also an important index, but it should be equal to (D1) as the upper structure is a rigid body. According to page limitation, only the test results, which used 12 ton's upper structure, are illustrated in this study. The completed test results can be found in the test report form NCREE.



the four earthquake records used in the shaking table test.

In order to facilitate comparison of results from a large number of experimental cases, Figures 8 shows the comparison of the maximum absolute acceleration (A1) and relative displacement (D1) of the hybrid controlled base-isolation system of passive and semi-active control cases with respective to the peak ground acceleration (PGA) levels. Plots in these figures for passive operation of the MR damper indicate only the two extremes of the voltage command levels, "P-0Vb" and "P-1Vb", which represent the "lose power" and "maximum power" condition respectively. First, it is apparent from these figures that the greater the constant command voltage that is sent to the MR damper in a passive mode, the larger the reduction in relative displacement. Secondly, although the relative displacement is well controlled in the maximum command voltage case "P-on", the control effect of the absolute acceleration is poor. In short word, lower command voltage (such as case "P-0Vb") to the MR damper will lead better absolute acceleration reduction. But the stroke will exceed the capacity of the MR damper when the input ground acceleration exceeds 200 gal. Higher command voltage (such as case "P-1Vb") to the MR damper will lead better displacement reduction. But the absolute acceleration is always poor in every PGA level. For semi-active control cases "S3", reductions in the maximum relative displacement are similar in magnitude to the "P-on" case that uses the maximum command voltage, and the absolute acceleration of the isolated structure (A1) is almost as small as the case ""P-0Vb". Moreover, since energy supplied to the MR damper can be reduced through use of modulated current, the semi-active control system provides a more efficient means of control than "P-1Vb" and also reduces the temperature of the MR fluid. In conclusion, the semi-active controlled base-isolation system which uses the fuzzy logical control algorithm can control both the relative displacement and absolute acceleration. It is the most adaptable control system to control the base-isolation system subject to different PGA levels of excitations. It can adjust the command voltage to the MR damper to reduce the absolute acceleration in different PGA levels of excitations without exceeding the stroke capacity of the base-isolation system. In the other hand, the

passive control cases can only control the relative displacement or the absolute acceleration. They are not



adaptable to against different kinds of excitations.

Figure 8: Comparison of the maximum absolute acceleration (A1) and relative displacement (D1) of the hybrid controlled base-isolation system with different control cases.

Time history of response from each transducer on the experimental structure provides additional data for interpretation of important phenomena. The discussion that follows first presents results from passive control and then those from semi-active control. The upper plot in Figure 9 shows the time history responses of the relative displacement of the passive-controlled ("P-1Vb") base-isolation system under El Centro earthquake excitation (PGA=0.4g). While the lower plot shows the comparison of the input ground acceleration (red line) and the absolute acceleration of the base-isolated structure (green line). According to this figure, the passive controlled base-isolation system can subject to 400 gal El Centro earthquake excitation without exceeding the stroke capacity of the base-isolation system. The relative displacement control effect is good, and the absolute acceleration reduction is reduced from 400gals to 170 gals (57% reduction).

Figure 10 shows the same comparison in the semi-active controlled base-isolation system ("S3"). The time history response of the relative displacement is similar to the passive case "P-1Vb" (See Figure 9). But, comparing the time history responses of the absolute accelerations, the maximum absolute acceleration response of the semi-active controlled base-isolated structure is greatly reduced from 400 gals to 80gals (80% reduction). It shows that the semi-active control system which uses the fuzzy logic control algorithm can reduce both the relative displacement and absolute acceleration responses under strong earthquake excitation. As the semi-active control system can optimal adjust the resistance of the MR damper online according to the system responses and semi-active controller, it is more effective and

efficient than the passive control systems.



Figure 9: Time history responses of the relative displacement (upper plot), input ground acceleration and isolated acceleration (lower plot) of the passive-controlled ("P-1Vb") base-isolation system under El Centro earthquake excitation (PGA=0.4g).



Figure 10: Time history responses of the relative displacement (upper plot), input ground acceleration and isolated acceleration (lower plot) of the semi-active controlled ("S3") base-isolation system under El Centro earthquake excitation (PGA=0.4g).

Figure 11 and 12 show the time history responses of the MR damper force (upper plot), command voltage (middle plot) and the hysteresis loops (lower left plot), force/velocity relationship of the MR damper in the passive ("P-1Vb") and semi-active ("S3") controlled base-isolation system under El Centro earthquake excitation. Comparing the time history responses of the MR damper forces in passive and semi-active control cases (see the upper plot in Figure 11 and 12); the damper force in passive mode is

always huge, while the damper force in semi-active mode is altered according to the excitation. Comparing the command voltage to the MR damper (the middle plots in Figure 11and 12). Passive case "P-1Vb" always uses the great command level (1 Volt) as input, as result, the damper force is always huge. The command voltage of in the semi-active control case "S3" is altered according to the feedbacks form the responses of the base-isolation system and the fuzzy logical control gain (or, control surface). It make the MR damper can do the optimal adjustment in each time step, consequently, the semi-active control system will has the best control efficiency. The lower plot in figure 11 and 12 show the hysteresis loops and force/velocity relationships of the passive and semi-active control system. In figure 11, the MR damper is work in passive mode, as results, the hysteresis loop is unique just like a passive damper. In figure 12, the hysteresis loop is changing all the time. The shape of hysteresis loop is not only decided by the characteristic of the MR damper has a bone shape. Which means, when the relative displacement is small the resistance of the MR damper is small to gain the better acceleration reduction. When the relative displacement is big, the resistance of the MR damper is big to mitigate the exceed displacement response.



Figure 11: Time history responses of the MR damper force (upper plot), command voltage (middle plot) and the hysteresis loops (lower left plot), force/velocity relationship of the MR damper in the passive controlled ("P-1V") base-isolation system under El Centro earthquake excitation (PGA=0.4g).



Figure 12: Time history responses of the MR damper force (upper plot), command voltage (middle plot) and the hysteresis loops (lower left plot), force/velocity relationship of the MR damper in the semi-active controlled ("S3") base-isolation system under El Centro earthquake excitation (PGA=0.4g).

CONCLUSIONS

This experimental study investigates performance of a hybrid base-isolation system that includes rolling pendulum system and a 20 kN MR damper. The system is tested on a large shaking table and numerous transducers monitor motion and feedback data to a controller. Fuzzy logic control is used to design the semi-active controller that modulates voltage to the MR damper. The goal is to mitigate response of the mass with the aid of the nonlinear base-isolation system. Different passive and semi-active control cases are used to test to the effectiveness of each strategy.

Conclusions from this study are summarized as follows:

- The rolling pendulum system is used as the isolator in this study. It can provide a suitable restoring force with almost no friction force. The damping force is only provided by the adjustable MR damper, and it maximizes controllable rang of the semi-active control system.
- The benefit of a semi-active controllable damper in a base-isolation system is evident, especially for protection against different kinds of levels of earthquakes. The most different between the passive and semi-active control system is that the semi-active control system is adaptable to various kinds and intensity of excitations. While the passive control system can only focus on some cases (P-1Vb: maximize the displacement control effect; P-0Vb: Maximize the acceleration reduction.).

- Fuzzy logic control is effective and easy to be applied to the semi-active control system. No inverse model for the MR damper is needed. As results, the calculation time is less; the stability of the semi-active controlled system is also proved.
- Semi-active controller, which considers both relative displacement and absolute acceleration, is the most effective controller used in this study. Not only can it control absolute acceleration for moderate levels of excitation, but it also mitigates relative displacement responses for large excitations and near-fault earthquakes.
- This study provides evidence of full-scale, real-time control and highlights several advantages of augmenting a common base-isolation system with a semi-active MR damper that is modulated with a fuzzy controller.

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