



CONSIDERATION OF COLLAPSE AND RESIDUAL DEFORMATION IN RELIABILITY-BASED PERFORMANCE EVALUATION OF BUILDINGS

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SUMMARY

The consideration of collapse and residual deformation in structural response analysis has been shown favorable in this study in view that performance-based design methodology could be successfully implemented in the near future to account for distinct nonlinear dynamic behavior of traditional structural systems and modern advanced structural systems with self-centering devices. In the framework of dual-level design, ordinary building stocks generally reach a structural state of near collapse at the 2% in 50 years hazard level. On the other hand, residual deformation, when combined with maximum deformation, has been shown effective in evaluation of structural performance under seismic excitation especially for advanced structural systems. To incorporate collapse and residual deformation in structural performance assessment, collapse experiments are recommended to establish such hysteretic models with post-peak material behavior.

INTRODUCTION

Performance-based seismic design philosophy has been recently incorporated into new generation code documents. To successfully implement dual-level design methodology, hysteretic models that take into account post-peak material behavior is favorable since ordinary building stocks generally reach a structural state of near collapse at the 2% in 50 years hazard level. On the other hand, with increasing use of modern advanced structural systems with self-centering devices, residual deformation, when combined with maximum deformation, has become very effective in assessment of structural performance under seismic excitation. Moreover, residual deformation is also a major concern to building owners and design engineers since it well represents the final status of building structures after earthquakes. As such, a conceptual Performance Matrix has been recently proposed in Pampanin et al. [1], using both maximum

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and residual deformations as performance evaluation indices. The reasons to evolve a currently popular and relatively simple evaluation method into a more knowledge-demanding performance evaluation method is based on an understanding of the following aspects:

1. The consideration of near-fault motions with severe directivity velocity pulses and/or static displacement fling could lead to permanent deformation of the structural system when highly nonlinear structural behavior occurs. Moreover, a 2% in 50 years hazard level usually make an ordinary structure almost reach its collapse state.
2. Buildings designed to older code documents are susceptible to severe damage or may even collapse during a severe seismic event. This is especially true for the observed low-cycle collapse of reinforced concrete frame buildings with light transverse column reinforcement during the 1999 Chi-Chi earthquake.
3. Modern advanced structural systems, in contrast to traditional systems, may be capable of re-centering itself back to the original position after earthquakes.

The former two aspects are the main concerns of this study, while one may refer to Pampanin et al. regarding the 3rd aspect on modern advanced structural systems. Modern advanced structural systems with re-centering device have inspired the use of residual deformation as an additional performance evaluation index in the near future. As we know, the current performance evaluation method is based on one or multiple structural response indices including maximum drift ratio (or, ductility) and cumulative inelastic energy dissipation, which are known to be able to fully characterize performance levels for systems where the main concern is to avoid collapse, but are unable to characterize the performance level of some modern structural systems (e.g., self centering frame buildings) where the structural integrity is not at risk during seismic attack. Besides, in the three aforementioned cases maximum response itself may not be able to fully represent the final status of the structure. As such, an independent scale of residual-deformation based performance measure can be effectively combined with the existing performance measure based on maximum response (or, cumulative damage) to form a more general performance domain. For different seismic intensity levels it would result in a full 3-dimensional performance domain, which is schematically described in Figure 1 (Pampanin et al.).

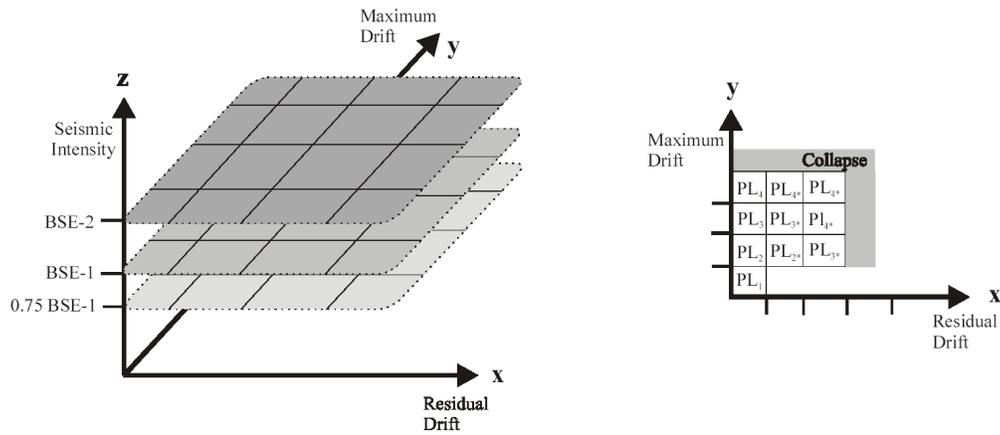


Figure 1. Framework for Residual-Maximum Performance Based Approach: Performance Matrix (source: Pampanin et al. 2003).

MATHEMATICAL FORMULATION OF HYSTERETIC MODEL WITH CONSIDERATION OF POST-PEAK BEHAVIOR

The governing equation of motion for an SDOF oscillator demonstrating hysteretic behavior can be expressed as:

$$m\ddot{x} + c\dot{x} + \alpha_n kx + k \sum_{i=1}^{n-1} \alpha_i u_i = -m\ddot{x}_g \quad (1)$$

where m is mass, c is viscous damping coefficient, k is initial stiffness of the system, α_i is post-to-preyield stiffness ratio (or, strain hardening ratio), u_i is auxiliary state variables, x_g is ground displacement, and x is relative displacement of the SDOF oscillator with respect to the ground. Dots indicate time derivative. The hysteretic models found in the literature to describe nonlinear behavior of deteriorating structural systems under cyclic loading can be categorized into three groups: (1) smooth hysteretic model, e.g., Wen [2], Baber and Noori [3], Wang and Wen [4], Sivaselvan and Reinhorn [5], etc.; (2) rule-based polygonal hysteretic model, e.g., Park et al. [6], Shi [7], Elwood [8], Ibarra et al. [9], etc.; (3) theory-based piecewise linear hysteretic model, e.g., Mostaghel [10], etc. In this study, a new theory-based piecewise linear model is proposed, and it can be used to define constitutive relationship between stress and strain, force and displacement, moment and curvature, or moment and rotation, depending on the applications as long as the quantity and quality of experimental results are sufficient for the determination of the values of key model parameters. The SDOF hysteretic system in Figure 2 contains one linear spring, the deformation of which is represented by x , and a slider-spring element with a frictional surface of variable Coulomb damping coefficient such that the slider-spring will start to slip at a certain force level (e.g., $k \cdot u_y$ at first yield). However, the slip may accelerate when the friction coefficient reduces to a lower level because of a decrease in the interlocking force between internal particles of the system, which, in the case of RC columns, physically means major shear cracks have fully developed. Such post-peak behavior is commonly observed in low-confinement RC columns, pre-Northridge steel connections, and wood shear wall system. To describe such a phenomenon, unknown u representing the deformation of the spring connected to the slider can be expressed in the following mathematical form:

$$\dot{u} = \dot{x} \cdot \left\{ \begin{array}{l} \bar{N}(\dot{x}) \cdot \left[\begin{array}{l} \phi_k \cdot \bar{M}(u - \lambda_p \cdot \phi_l \cdot \delta_y^+) \cdot \bar{M}(x) + \phi_k \cdot \bar{M}(u - \phi_l \cdot \delta_y^+) \cdot \bar{N}(x) \\ + (-\phi_c^+ - \phi_k) \cdot \bar{N}(x - \delta_u^+) \cdot \bar{M}(x - \delta_r^+) \cdot N(u) \cdot N(x - \delta_{FS}^+) \\ + (-\phi_r^+ - \phi_k) \cdot \bar{N}(x - \delta_r^+) \cdot N(u) \cdot N(x - \delta_{FS}^+) \end{array} \right] \\ + M(\dot{x}) \cdot \left[\begin{array}{l} \phi_k \cdot N(u + \lambda_p \cdot \phi_l \cdot \delta_y^-) \cdot N(x) + \phi_k \cdot N(u + \phi_l \cdot \delta_y^-) \cdot M(x) \\ + (-\phi_c^- - \phi_k) \cdot M(x + \delta_u^-) \cdot N(x + \delta_r^-) \cdot \bar{M}(u) \cdot N(-x - \delta_{FS}^-) \\ + (-\phi_r^- - \phi_k) \cdot M(x + \delta_r^-) \cdot \bar{M}(u) \cdot N(-x - \delta_{FS}^-) \end{array} \right] \end{array} \right\} \quad (2)$$

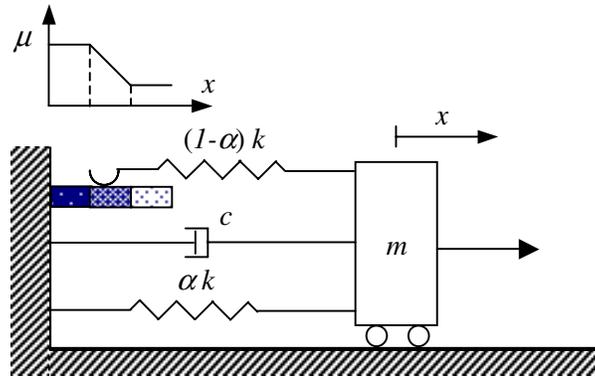


Figure 2. Schematic representation of SDOF hysteretic system with consideration of post-peak behavior.

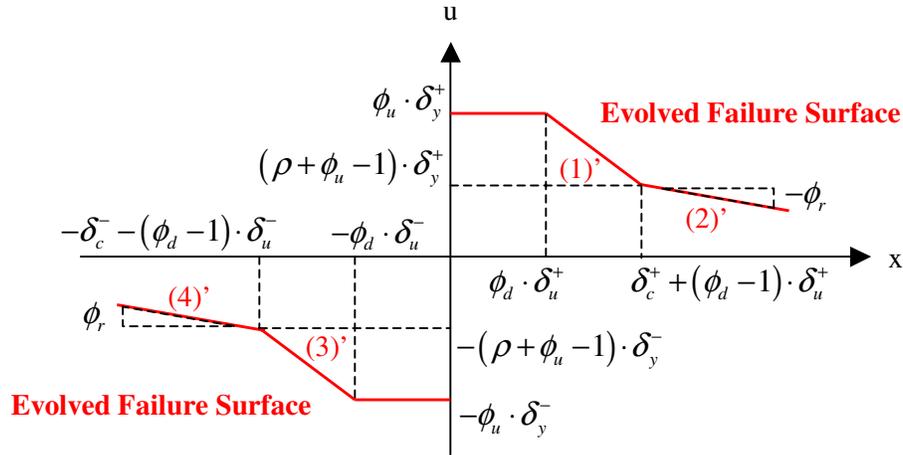


Figure 4. Evolution of failure surface and its controlling parameters.

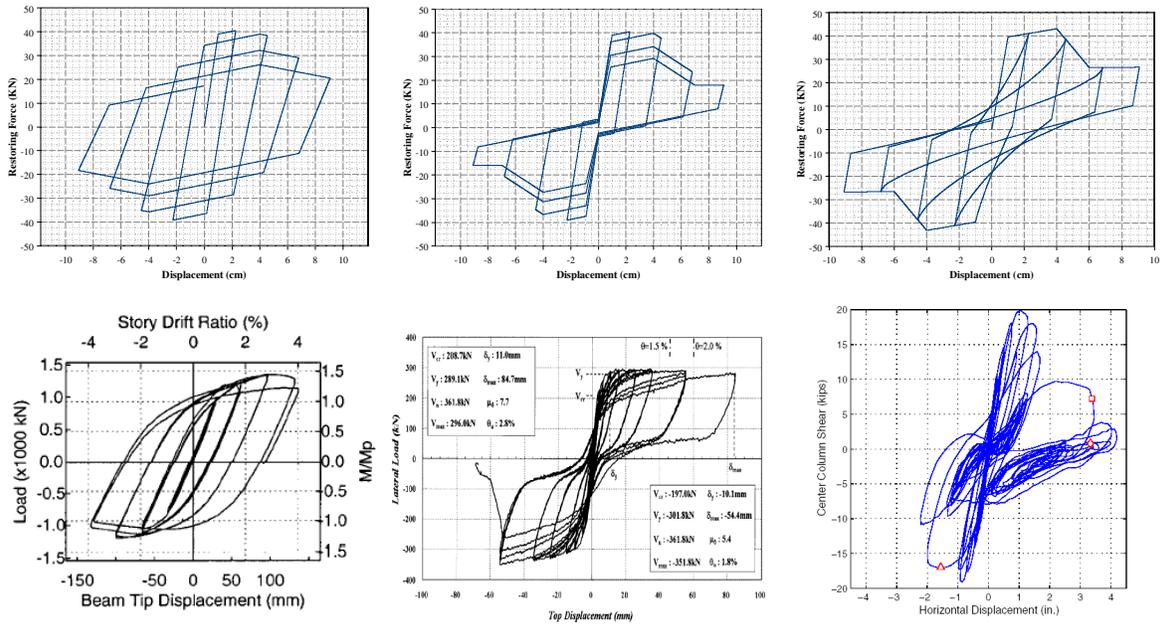


Figure 5. Numerical hysteretic models having post-peak negative stiffness (upper row) and experimental results showing similar characteristics (lower row, from left to right, after Uang et al. [11], Oh et al [12], and Elwood [8]).

PERFORMANCE EVALUATION METHOD CONSIDERING PEAK AND RESIDUAL DEFORMATIONS

A preliminary study has been conducted, and numerical results show that collapse consideration is essential in order to implement the newly proposed Performance Matrix in the next generation design codes. Experience shows that peak and residual deformations can be predicted with accuracy only if post-peak negative stiffness and collapse are taken into account in structural response analysis. Collapse analysis on a 12-story RC building is presented as an example in the following.

Description of 12-story RC Model Building

A 12-story RC building with a natural period of 1.61 sec was designed in Liao and Wang [13]. The building has a 25cm yield displacement and a 10% pre-to-postyield stiffness ratio according to static pushover analysis results. 5% viscous damping of critical is assumed. To perform collapse analysis on the building, an equivalent SDOF system using base shear formulation suggested by Collins et al. [14] is used. Reliable estimate of global (roof) drift ratio of the building is expected using the suggested procedure. For non-deteriorating bilinear system, $\phi_k = 1$, $\phi_l = 1$, $\lambda_k = 0$, $\lambda_l = 0$ and $\lambda_p = 1$. $\lambda_p = 0.3$ is assumed for pinching system; $\lambda_k = 1$ and $\lambda_l = 0.1$ for deteriorating system. $\rho = 0.25$ is assumed for residual strength. When collapse is a concern, $\delta_u = 4\delta_y$, $\delta_r = 6\delta_y$, and $\phi_r = 0.1$ is assumed for the system.

Suites of Uniform Hazard Ground Motions

Design spectra corresponding to 2 hazard levels of Design and Maximum Considered Earthquakes from the Taiwanese seismic design code are constructed in Figure 6 to represent the base shear coefficients of the Xinyi district of Taipei basin. According to probabilistic seismic hazard analysis results (Jean [15]), an intermediate hazard level of 5% exceedance probability in 50 years is added to our response analyses. To get 10 uniform hazard earthquake motions at each hazard level, TSMIP array data in Taipei basin within a time frame of 1994 ~ 2002 are selected to match the design spectra in a wide range of periods. Important characteristics of these selected motions are summarized in Tables 1 through 3. The scaling factors are preferentially no larger than 12.61, which imply that no small magnitude earthquakes are taken to represent much higher hazard levels of large magnitude earthquakes. Due to the limitation of data obtained from the field, it is observed that most of the selected motions are from the 1999 Chi-Chi earthquake and the March 31, 2002 Hualien earthquake. Median, 16- and 84-percentile spectra of the 10 selected motions are plotted against the target design spectra for comparison (Figure 6).

Table 1. Important characteristics of 10 earthquake motions in the 10% in 50 years hazard level.

Date (GMT)	M _L	Focal Depth (km)	Station ID	Duration (sec)	PGA (g)	Scaling Factor
1995/6/25	6.5	39.9	TAP008	92	0.050	8.47
1999/9/20	7.3	8.0	TAP	60	0.042	3.28
1999/9/20	7.3	8.0	TAP005	134	0.083	1.74
1999/9/20	7.3	8.0	TAP007	134	0.071	2.42
1999/9/20	7.3	8.0	TAP083	120	0.035	5.23
1999/9/20	7.3	8.0	TAP051	90	0.071	3.25
2000/9/10	6.2	17.7	TAP050	70	0.027	8.28
2002/3/31	6.8	13.8	TAP094	95	0.045	4.20
2002/3/31	6.8	13.8	TAP044	75	0.062	2.50
2002/3/31	6.8	13.8	TAP015	90	0.130	1.50

Table 2. Important characteristics of 10 earthquake motions in the 5% in 50 years hazard level.

Date (GMT)	M _L	Focal Depth (km)	Station ID	Duration (sec)	PGA (g)	Scaling Factor
1995/6/25	6.5	39.9	TAP008	92	0.050	9.55
1999/9/20	7.3	8.0	TAP	60	0.042	3.70
1999/9/20	7.3	8.0	TAP083	120	0.035	5.90
1999/9/20	7.3	8.0	TAP047	87	0.079	4.24
2002/3/31	6.8	13.8	TAP075	76	0.056	6.67
2002/3/31	6.8	13.8	TAP044	75	0.040	4.10
2002/3/31	6.8	13.8	TAP044	75	0.062	2.82
2002/3/31	6.8	13.8	TAP040	79	0.052	4.25
2002/3/31	6.8	13.8	TAP110	87	0.065	2.90
2002/3/31	6.8	13.8	TAP015	90	0.130	1.70

Table 3. Important characteristics of 10 earthquake motions in the 2% in 50 years hazard level.

Date (GMT)	M _L	Focal Depth (km)	Station ID	Duration (sec)	PGA (g)	Scaling Factor
1995/6/25	6.5	39.9	TAP008	92	0.050	12.61
1999/9/20	7.3	8.0	TAP100	144	0.065	4.32
1999/9/20	7.3	8.0	TAP083	120	0.035	7.79
1999/9/20	7.3	8.0	TAP051	90	0.071	4.84
1999/9/10	6.2	17.7	TAP050	70	0.027	12.33
2002/3/31	6.8	13.8	TAP094	95	0.045	6.25
2002/3/31	6.8	13.8	TAP044	75	0.040	5.42
2002/3/31	6.8	13.8	TAP044	75	0.062	3.73
2002/3/31	6.8	13.8	TAP041	84	0.076	4.73
2002/3/31	6.8	13.8	TAP015	90	0.130	2.24

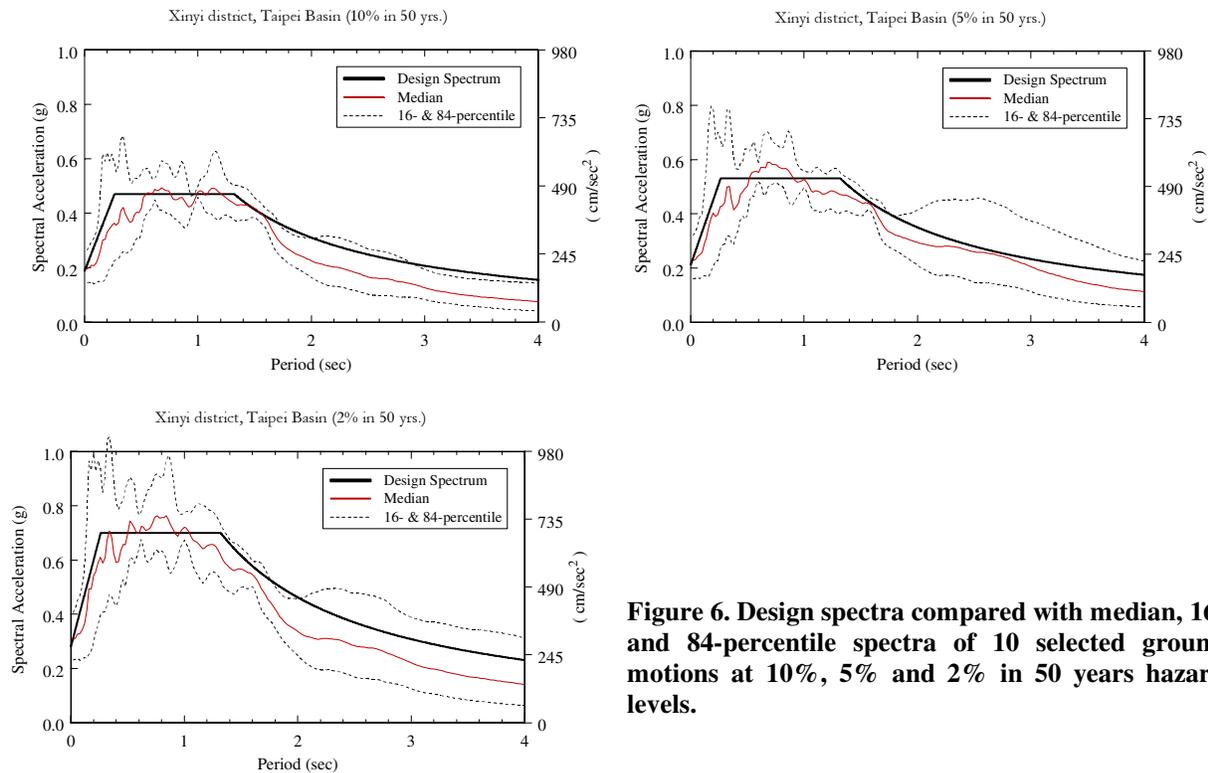


Figure 6. Design spectra compared with median, 16- and 84-percentile spectra of 10 selected ground motions at 10%, 5% and 2% in 50 years hazard levels.

Nonlinear Time History Analysis and Engineering Implications

Nonlinear time history analysis is performed on the equivalent SDOF system to yield estimates of maximum and residual roof drift ratios of the 12-story RC building using the 5th order Cash-Karp Runge-Kutta method to implement adaptive time stepping algorithm. Numerical results are given in the format of Performance Matrix. Although not significant, the bilinear system generally has a lower level of maximum drift ratios, but its residual drift ratio is slightly higher. This is because in this study an identical level of strength deterioration and stiffness degradation is assumed for bilinear and pinching systems. Comparisons are also made in system responses with and without consideration of collapse mechanism. It is observed that response estimates at the 10% in 50 years level coincide for both cases

since collapse, mostly, does not occur. However, as long as 2% in 50 years hazard level is of concern, the response estimate will strongly depend on whether collapse is taken into consideration. This observation surely has very important implications in seismic design, and performance evaluation of structural systems under seismic excitation. If the use of Performance Matrix is a necessity in the framework for performance-based earthquake engineering, then the consideration of collapse in dynamic analysis will help map a structure's performance into its corresponding Performance Level cells with confidence, as shown in Figure 1. In passing, it is noted that the traditional analysis approach usually provides only information on whether the building collapses according to engineering judgment and experience, but a confident estimate of maximum and residual drift is not possible.

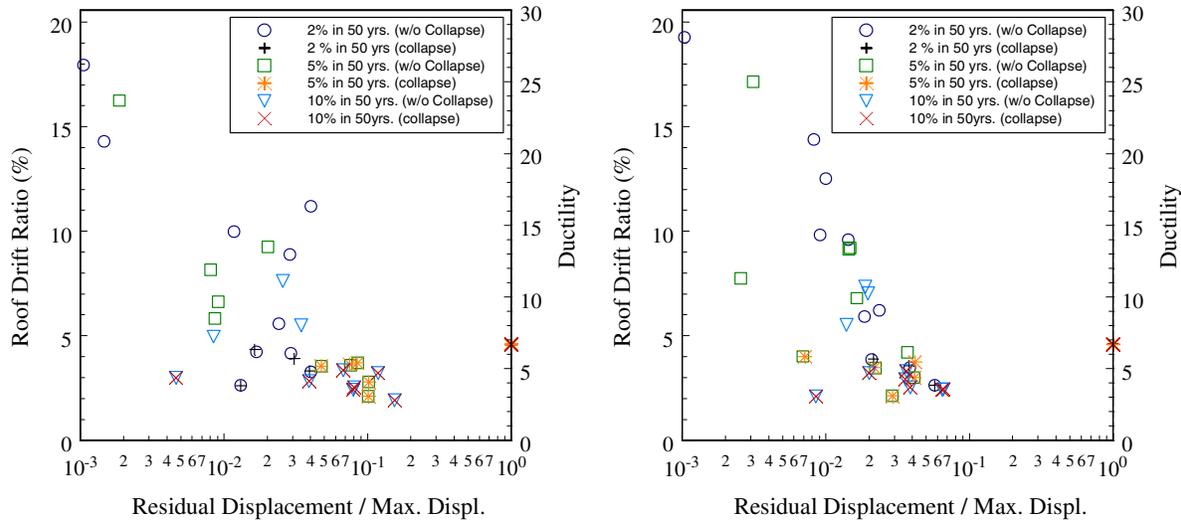


Figure 7. Performance Matrix of the 12-story RC model building with bilinear (left) and pinching (right) hysteretic behavior.

SHAKE TABLE TEST ON RC FRAME WITH LOW-DUCTILITY COLUMNS

A series of shake table tests are desirable in order to validate the proposed piecewise linear hysteretic model, and experimental results could be very supportive in determination of key parameter values. Although not many, a few collapse experiments had been conducted to this date. Among those are gravity load collapse of 1/2-scale RC frames by Elwood [8] and small-scale steel frame tests by Vian et al. [16]. To investigate how the 4-story commercial-resident complexes sustained severe damage and some of them even collapsed in the 1999 Chi-Chi earthquake, a 1/2-scale RC frame composed of 2 low-ductility columns inter-connected by a strong beam (Figure 8) was tested on the shake table earlier in February 2004. The frame specimen originates from the collapse experiments by Elwood with a few modifications to account for:

1. Realistic vertical deformation on columns of the frame specimen with no alternative path for load redistribution.
2. Typical 4-story commercial-resident buildings since the column design is taken from a real 4-story building in central Taiwan.
3. Soft 1st story design that is commonly observed for the 4-story commercial-resident complexes in Taiwan, and during the 1999 Chi-Chi earthquake a large number of such buildings sustained damage only at the 1st story.

The NS component of TCU076 accelerogram recorded during the 1999 Chi-Chi earthquake was applied to excite the frame specimen of a 0.35sec natural period, representing a 0.49sec commercial-resident

complex at full-scale. TCU076, stationed at Nantou Elementary School, is less than 250m from the 4-story target building. The specimen was subjected to a sequence of TCU076 records, scaled from 25gal to 700 gal to obtain hysteretic behavior of the specimen. The achieved table motion of TCU076 and its response spectrum are given in Figure 9. Two hysteretic loops are shown in Figure 10, corresponding to intensity levels of 50gal and 700gal, respectively. At the end of the experiments, the natural period of the frame specimen lengthened to 0.64sec. Only bending cracks were observed during the test, which agrees with the reconnaissance report of the target building after the 1999 Chi-Chi earthquake. Such design, representing an upper bound of the building performance in central Taiwan, did help prevent the building from collapse during a severe earthquake event. In order to collect more experimental data for validation of the proposed hysteretic model, two more shake table tests are under preparation and they are expected to yield helpful data such that considerable improvements can be achieved on numerical dynamic analysis of structural collapse in the near future.

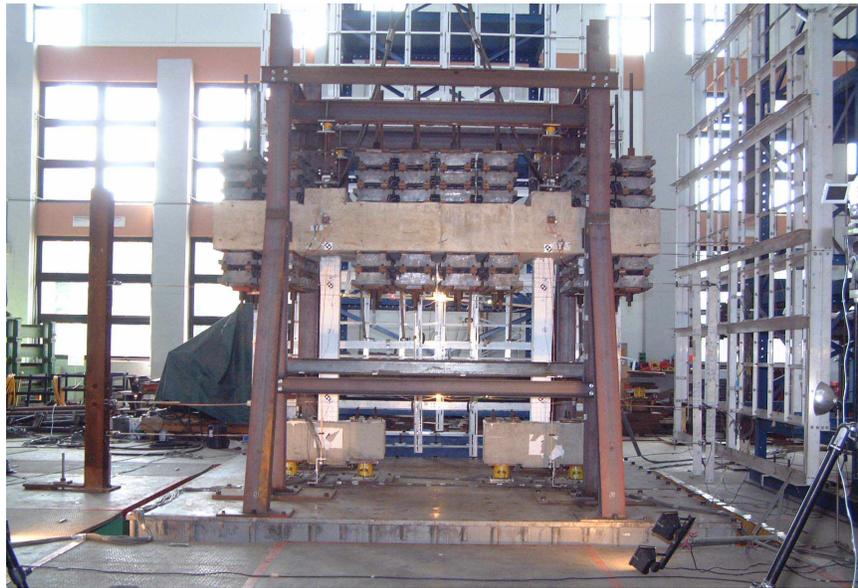


Figure 8. Front view of the experimental setup of the low-ductility RC frame.

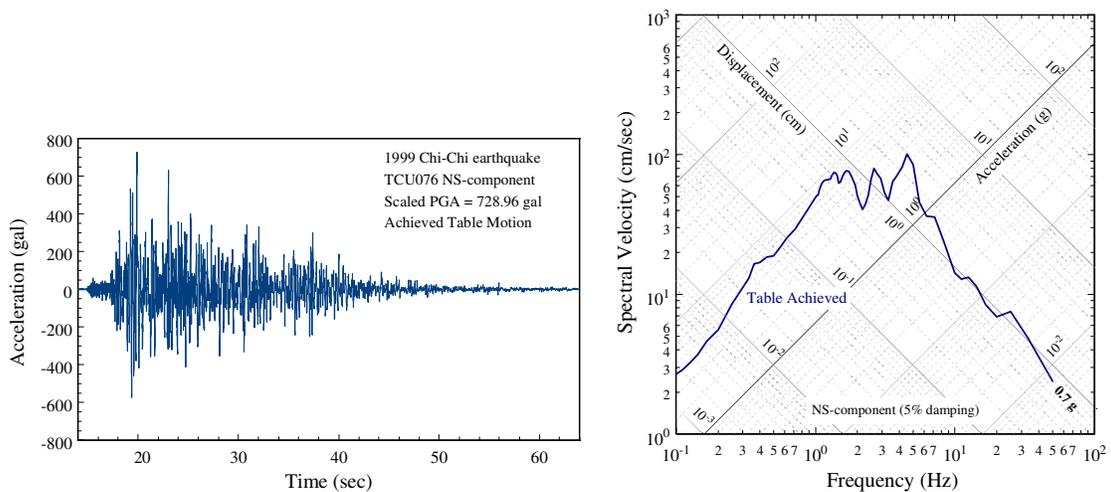


Figure 9. Recorded table motion (left) and its response spectrum (right).

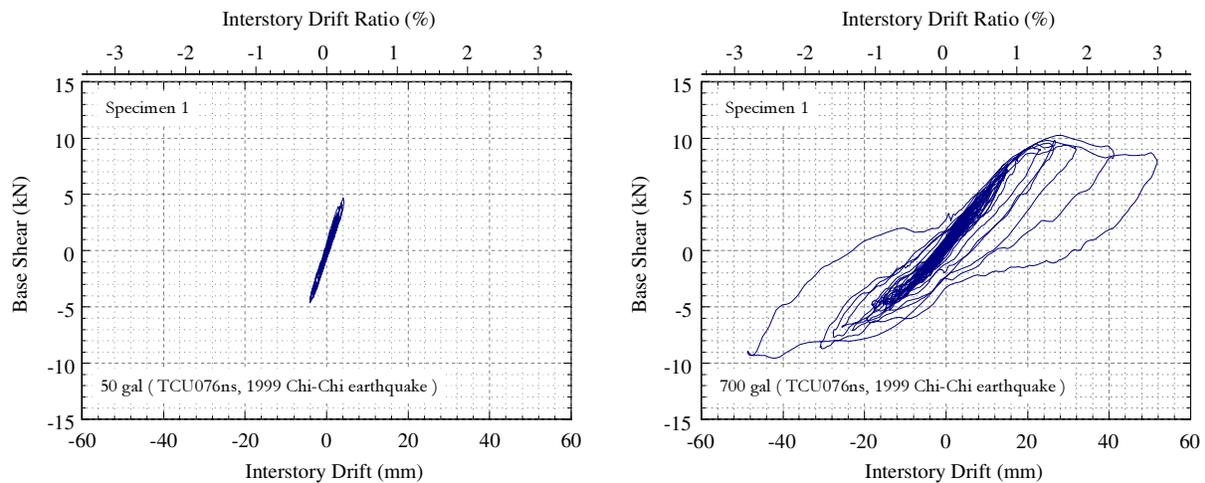


Figure 10. Sample hysteretic loops of reinforced concrete frame specimen subjected to TCU076ns record of the 1999 Chi-Chi earthquake scaled to 50 gal (left) and 700gal (right) intensity levels.

CONCLUSIONS

The preliminary finding of this ongoing study is the introduction of performance-based earthquake engineering into the seismic design documents has indicates the needs of considering post-peak behavior of structural systems in nonlinear dynamic analysis especially at the hazard level of very rare events such as 2% exceedance probability in 50 years. To do so, a new mathematical form is presented in this study to describe hysteretic loops with post-peak behavior. Unlike other rule-based models, the proposed mathematical form can be readily embedded into existing in-house and commercial software with no excessive coding efforts. It is also shown that collapse consideration is necessary for ordinary building stocks if Performance Matrix is to be incorporated into the next generation design codes.

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