



PRACTICAL EXPERIENCE USING A SIMPLIFIED PROCEDURE TO MEASURE AVERAGE SHEAR-WAVE VELOCITY TO A DEPTH OF 30 METERS (V_{s30})

Antony J. MARTIN¹ and John G. DIEHL²

SUMMARY

V_{s30} is used in the NEHRP Provisions and the 1997 Uniform Building Code to separate sites into classes for earthquake engineering design. V_{s30} can also be incorporated into local seismic hazard maps. Surface wave methods have been used to estimate V_{s30} for a number of years. These methods are non-destructive, and sample a larger volume of the subsurface as compared to borehole measurements.

During the recent three years the authors have had the opportunity to test a simplified procedure to estimate V_{s30} and compare the results to complete surface wave soundings and borehole measurements. Here the authors present the results of these comparisons, practical applications of this method, and the results for engineering practice.

INTRODUCTION

Shear-wave velocity (V_s) has long been known to be an essential parameter for evaluating the dynamic properties of soils. The average shear-wave velocity in the top 30 m, based on travel time from the surface to a depth of 30 m, is known as V_{s30} . V_{s30} is used in the NEHRP Provisions (BSSC, 1994) and the 1997 Uniform Building Code to separate sites into different classes for engineering design, with the expectation that sites in the same class will respond similarly to a given earthquake. The 2000 International Building Code (IBC) permits a similar approach for site classification, the average shear wave velocity of the upper 100 ft. These site classes are as follows:

- Class A – hard rock – $V_{s30} > 1500$ m/s (UBC) or $V_{s100'} > 5,000$ f/s (IBC)
- Class B – rock – $760 < V_{s30} \leq 1500$ m/s (UBC) or $2,500 < V_{s100'} \leq 5,000$ f/s (IBC)
- Class C – very dense soil and soft rock – $360 < V_{s30} \leq 760$ m/s (UBC)
or $1,200 < V_{s100'} \leq 2,500$ f/s (IBC)
- Class D – stiff soil – $180 < V_{s30} \leq 360$ m/s (UBC) or $600 < V_{s100'} \leq 1,200$ f/s (IBC)
- Class E – soft soil – $V_{s30} < 180$ m/s (UBC) or $V_{s100'} < 600$ f/s (IBC)
- Class F – soils requiring site-specific evaluation

Other applications of V_s imaging include seismic risk or PML studies, seismic hazard zonation, and characterization of seismic instrument sites.

¹ Technical Director, GEOVision Geophysical Services, Corona, California. amartin@geovision.com

² Vice President, GEOVision Geophysical Services, Corona, California. Email: jdiehl@geovision.com

Traditionally, V_{s30} is determined by seismic measurements in boreholes, using the downhole, crosshole, or suspension logging methods. Techniques based on the inversion of surface-wave dispersion data offer the advantage of not requiring boreholes and sampling of a larger volume of soil.

Surface wave techniques such as the spectral-analysis-of-surface-waves (SASW), multi-channel analysis of surface waves (MASW), array microtremor and refraction microtremor techniques are proven, non-destructive seismic methods that can be used to determine the variation of V_s with depth (Stokoe et al., 1994; Brown, 1998; Park et al., 1999; Okada, 2003 and Louie, 2001). The basis of surface wave methods is the dispersive characteristic of Rayleigh waves when propagating in a layered medium. The Rayleigh-wave phase velocity primarily depends on the material properties (shear-wave velocity, compression-wave velocity or Poisson's ratio, and mass density) to a depth of one wavelength. The variation of phase velocity with frequency or wavelength is called dispersion. Surface wave testing consists of collecting surface-wave phase data in the field, generating the dispersion curve, and then using iterative forward or inverse modeling techniques to back-calculate the corresponding V_s profile. From the V_s profile, V_{s30} can be calculated.

THEORETICAL BASIS OF V_{s30} METHOD

The V_{s30} method presented herein is a simplification of other surface wave methods, providing only a single number corresponding to the average shear-wave velocity in the upper 30 m. A method based on the SASW technique was first introduced by Brown et al. (2000a and 2000b) and a similar method based on the passive array microtremor technique was developed independently by Konno and Kataoka (2000).

In the V_{s30} method, data acquisition can be less extensive and faster relative to complete surface wave soundings because only a portion of the dispersion curve is needed. The analysis is simple enough that a preliminary interpretation can be made on site. The method is based on the correlation between Rayleigh-wave phase velocity and V_{s30} , as described below. Like V_{s30} , Rayleigh-wave phase velocities depend on the material properties averaged over depth. The field procedure consists of measuring only those phase velocities necessary to accurately estimate V_{s30} using an empirical predictive equation.

The predictive equation was developed by Leo Brown (Brown et al., 2000a and 2000b) using linear regression on a set of Rayleigh-wave dispersion curves and V_{s30} values that were calculated from seismic velocity profiles. Profiles were selected that contained shear- and compression-wave velocity (V_p) data from the surface to a depth of approximately 80 m or more. Of the 103 profiles, 33 were obtained by the downhole seismic method, 66 by P-S suspension logging, and four unknown. Fifty of the sites are located in Southern California, 43 in Northern California, and 10 outside of California.

For each V_s , V_p profile, the fundamental-mode Rayleigh-wave dispersion curve was calculated. A constant mass density of 1.92 g/cc for each profile was assumed. Reasonable variations in mass density have a negligible effect on dispersion.

From the 103 profiles, data from 15 profiles were randomly selected and removed from the data set. Simple linear regression was done on the data from the remaining 88 profiles. Correlation was done in the wavelength rather than frequency domain, because wavelength is related more closely to depth of interest. V_{s30} is most highly correlated with the Rayleigh-wave phase velocity at a wavelength of 40 m (V_{R40}). The regression plot and residuals are shown in Figures 1a and 1b respectively. The degree of correlation is high ($r^2 = 0.9864$) and the standard error is 14.5 m/s. Fixing the constant (y-intercept) at 0 had an insignificant effect on the regression. Based on the regression, the predictive equation for V_{s30} is:

$$V_{s30} = 1.045 * V_{R40}. \quad (1)$$

The error bounds are approximately $\pm 10\%$ of the estimate for a 95% confidence interval. Multiple linear regression does not improve the correlation appreciably.

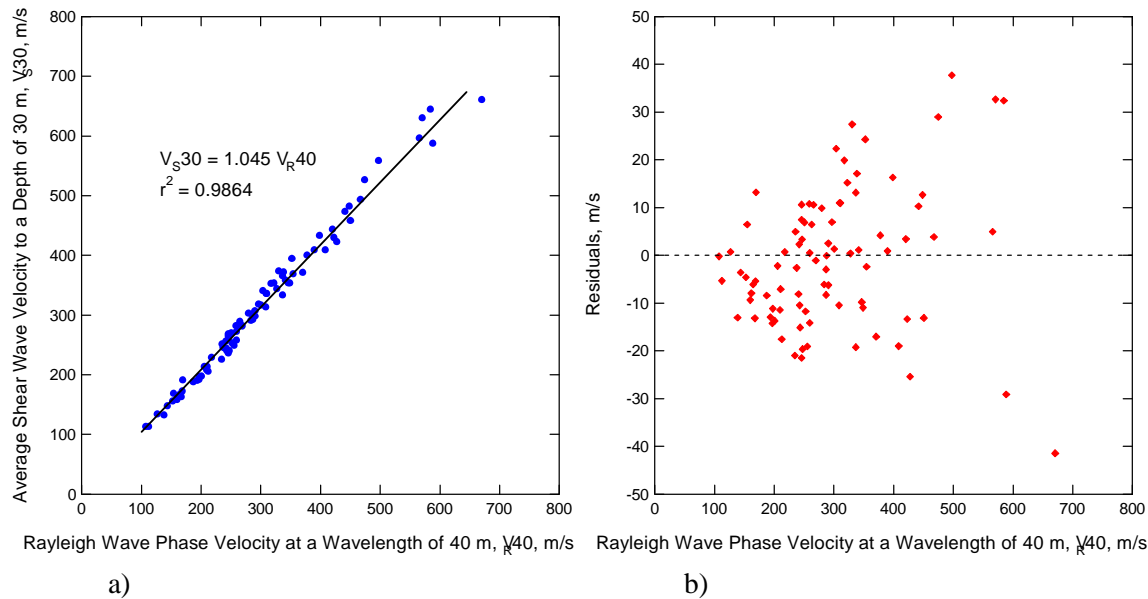


Figure 1. a) V_{S30} versus V_{R40} , with regression line and equations given. b) Residuals.

To evaluate the reliability of the V_{S30} regression equation, Brown et al. (2000a, 2000b) applied it to the dispersion curves from the 15 profiles not included in the regression. The predicted values of V_{S30} are compared with the actual values in Table 1. Values of V_{S30} are predicted within 5% and the site classifications are correct. This comparison assumes perfect data – that fundamental-mode Rayleigh waves are generated in a layered halfspace and that their velocity can be measured accurately.

Table 1. Evaluation of V_{S30} method based on V_S profiles not included in regression database

Site Name	V_{S30}	Predicted V_{S30}	Percent Error	Actual Site Class	Predicted Site Class
192	172	176	1.8	E	E
269	271	273	0.7	D	D
CPB	250	244	-2.7	D	D
OV2	441	426	-3.3	C	C
SOP	302	301	-0.1	D	D
WVAS	397	391	-1.4	C	C
PP1	400	417	4.5	C	C
USD	493	490	-0.6	C	C
DHS	380	376	-1.1	C	C
HAV	296	295	-0.3	D	D
HEA	241	242	0.6	D	D
SG4	304	314	3.4	D	D
SG5	334	341	1.9	D	D
SR4	345	340	-1.4	D	D
SC1	316	320	1.2	D	D

THE V_{s30} METHOD

Because only one point in the dispersion curve, V_{R40} , is needed to estimate V_{s30} , the standard surface wave testing procedures are simplified. For example, to measure V_{R40} using the SASW technique, only a single source-receiver spacing is needed. The seismic source must have sufficient energy for this distance and wavelength. Passive techniques such as the array microtremor and refraction microtremor techniques may also be used to determine V_{R40} . Typically, passive techniques must be used in conjunction with active techniques (SASW and MASW) in order to define the near surface velocity structure, which may have a significant impact on V_{s30} .

For sites where the shear-wave velocity profile generally increases with depth, the measured dispersion curve using the SASW technique is a good approximation of the fundamental-mode Rayleigh-wave dispersion curve (Foinquinos, 1991; Brown, 1998). Common exceptions to this situation include engineered fill over soft sediments, asphalt/concrete and compacted base material over softer sediments, and soft soil on shallow high velocity bedrock. At such sites higher mode surface waves may dominate and the predictive V_{s30} equation, which is based on fundamental-mode Rayleigh wave propagation may not be valid. The MASW technique can often be used to isolate the fundamental-mode Rayleigh-dispersion curve from higher modes (Park et al., 1999) and should be used in environments where velocity inversions or steep velocity gradients are expected.

The general testing setup for the V_{s30} method using SASW is shown in Figure 2 and summarized below. A vertical dynamic load at the surface generates predominantly Rayleigh waves, which are monitored by two receivers. A dynamic signal analyzer records the ground motions, transforms the time-domain records into the frequency domain, and calculates the cross power spectrum and coherence.

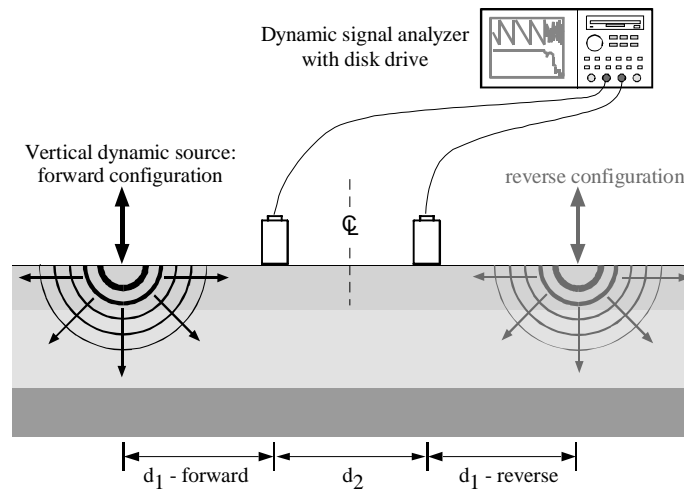


Figure 2. Basic field setup for V_{s30} measurements using the SASW technique.

After the wrapped phase angle of the cross power spectrum is unwrapped through an interactive process called masking, the dispersion curve is calculated by:

$$V_R = f * d_2 / (\Delta\phi / 360^\circ), \quad (2)$$

where f is frequency, d_2 is the distance between receivers, and $\Delta\phi$ is the unwrapped phase of the cross power spectrum.

As stated earlier, for this new V_{s30} method, a single source-receiver spacing is used. Based on practical and theoretical considerations (Sanchez-Salinerio, 1987), d_1 and d_2 both equal to 30 m or more would be adequate for measuring V_{R40} . To minimize phase shifts due to differences in receiver coupling and lateral variability, the source location is also reversed. Eq. 2 is used to calculate a short segment of the dispersion curve, which is smoothed to obtain V_{R40} . Eq. 1 is then applied to estimate V_{s30} .

MASW data is typically acquired using a linear array of 24 to 48 geophones spaced 1 to 2m apart. The source location is typically 2 m, or more, from the end geophone and filtering techniques such as the f-k or tau-p transforms are used to extract the dispersion curve from the field data. The MASW technique is also easily adapted to 2-D mapping of shallow shear wave velocity structure.

Standard field procedures are used to acquire and reduce array microtremor data (Okada, 2003) and refraction microtremor data (Louie, 2001). Array microtremor data is often acquired using a 7- or 10-channel triangular array or a 24 channel circular array. The refraction microtremor array typically uses a linear array of 24 geophones spaced 7 to 10 m apart and assumes that surface wave energy is arriving equally from all directions. The dispersion curve is determined using various filtering techniques, V_{R40} measured from the resulting dispersion curve and Eq. 1 then used to estimate V_{s30} . This eliminates the need to acquire SASW or MASW data to define near surface velocity structure and forward/inverse modeling of the dispersion curve to generate a V_s versus depth model.

An example of determining V_{R40} from a SASW and refraction microtremor sounding and comparison to actual V_{s30} calculated from forward modeling of the surface wave dispersion curve and PS suspension log data is presented in Figure 3.

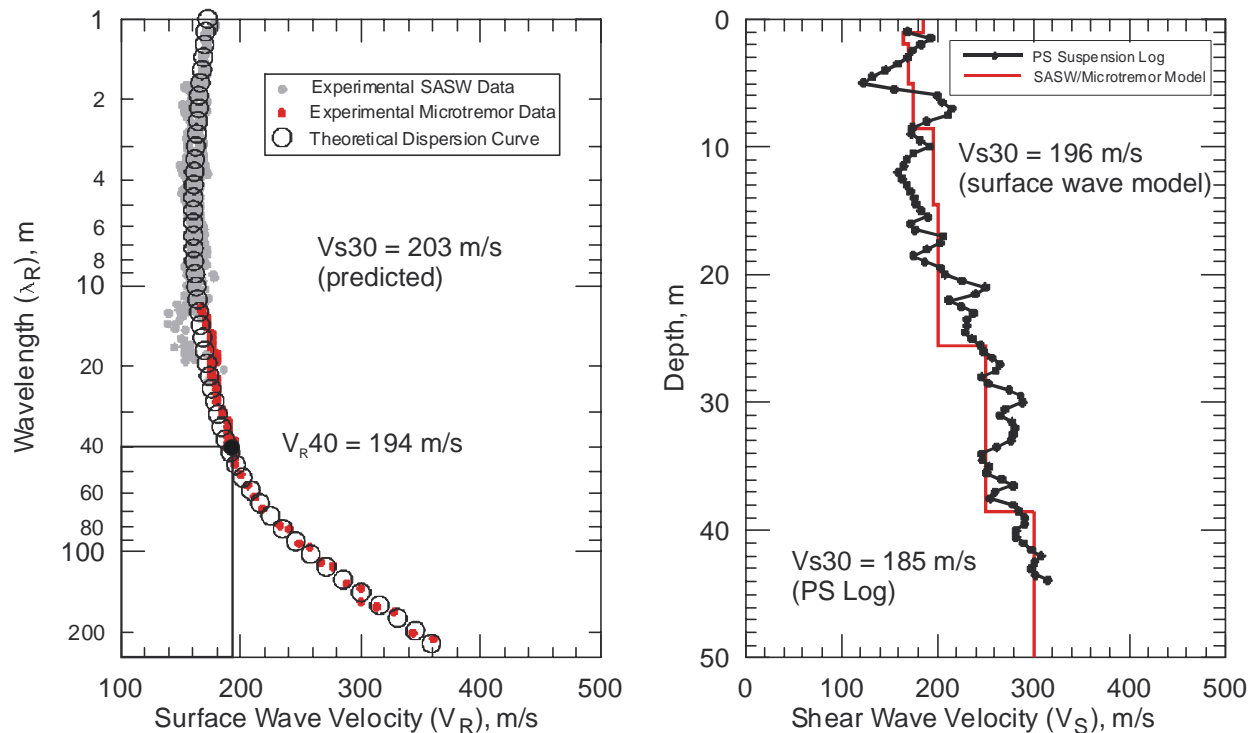


Figure 3. Example of V_{s30} calculation from SASW and refraction microtremor data.

The predicted V_{s30} is within 7 m/s (3%) of that determined from modeling of the surface wave dispersion curve and 18 m/s (10%) of that derived from PS suspension log V_s data.

EVALUATION OF THE V_{s30} METHOD

Over the past several years, the V_{s30} predictive regression equation has been applied to surface wave sounding data acquired at numerous sites in and outside of California and compared to V_{s30} determined by modeling of surface wave data and occasionally PS suspension logs. Most of the surface wave data were acquired using the SASW technique but recently we have been combining SASW soundings with passive array microtremor or refraction microtremor soundings to extend depth of investigation. The predicted values of V_{s30} from these investigations are compared to actual values in Table 2, below.

Table 2. Evaluation of V_{s30} method based on 53 new V_s profiles acquired since 2001.

Site Name	Actual V_{s30}^1	Predicted V_{s30}	Percent Error	UBC Site Class	Predicted UBC Site Class	Comments
San Diego, CA - A	229	248	8	D	D	groundwater (gw) @ 3m
Arrowhead, CA	360	376	4	C	C	weathered rock @ 20m
Stanford, CA - A	375	392	5	C	C	gw @ 14m
Stanford, CA - B	374	382	2	C	C	gw @ 14m
UC Davis A	230	230	0	D	D	gwr @ 13m
UC Davis B	232	220	-5	D	D	gw @ 13m
San Diego, CA - B	597	658	10	C	C	sedimentary rock @ 2-7m
UC Berkley A	386	387	0	C	C	sedimentary rock @ < 20m
UC Berkley B	437	481	10	C	C	sedimentary rock @ < 20m
San Diego, CA - C	292	330	13	D	D	gw @ 4.5m
San Diego, CA - D	298	310	4	D	D	gw @ 4.5m
Simi Valley, CA - A	192	201	5	D	D	gw @ 6m
Simi Valley, CA - B	246	269	9	D	D	gw @ 6m
Sakhalin Island, Russia - A	322	355	10	D	D	
Sakhalin Island, Russia - B	305	298	-2	D	D	
Sakhalin Island, Russia - C	332	327	-2	D	D	
Sakhalin Island, Russia - D	181	190	5	D	D	gw @ 1 m
Sakhalin Island, Russia - E	282	277	-2	D	D	gw @ 4 m
San Quentin, CA - A	872	726	-17	B	B	bedrock at 3-4m
San Quentin, CA - B	840	756	-10	B	B	bedrock at 3-4m
Rialto, CA - A	426	450	6	C	C	sand/gravel pit site
Rialto, CA - B	444	475	7	C	C	sand/gravel pit site
Rialto, CA - B	441	461	4	C	C	sand/gravel pit site
Sacramento, CA - A	344	355	3	D	D	gw @ 10m
Sacramento, CA - B	407	418	3	C	C	gw @ 10m
Dillon, CO - A	512	507	-1	C	C	gw @ 12m, sed rock @ 22m
Dillon, CO - B	493	530	7	C	C	gw @ 13m, sed rock @ 24m

Site Name	Actual V _{s30} ¹	Predicted V _{s30}	Percent Error	UBC Site Class	Predicted UBC Site Class	Comments
Dillon, CO - C	495	515	4	C	C	gw @ 13m, sed rock @ 24m
Dillon, CO - D	484	506	4	C	C	gw @ 13m, sed rock @ 24m
Fresno, CA - A	461	481	4	C	C	sand/gravel pit site, gw @ 3m
Fresno, CA - B	461	493	7	C	C	sand/gravel pit site, gw @ 3m
Fresno, CA - C	447	500	12	C	C	sand/gravel pit site, gw @ 3m
Irwindale, CA - D1	362	382	6	C	C	sand/gravel pit site, gw @ 43m
Irwindale, CA - D2	319	331	4	D	D	sand/gravel pit site, gw @ 2m
Irwindale, CA - H1	374	399	7	C	C	sand/gravel pit site, gw @ 9m
Irwindale, CA - H2	441	452	3	C	C	sand/gravel pit site, gw @ 51m
Irwindale, CA - R1	567	575	1	C	C	sand/gravel pit site, gw @ >50m
Irwindale, CA - R2	545	557	2	C	C	sand/gravel pit site, gw @ >20m
Irwindale, CA - U1	452	470	4	C	C	sand/gravel pit site, gw @ >30m
Irwindale, CA - U2	395	448	13	C	C	sand/gravel pit site, gw @ 2m
Martin County, KY - A	250	282	13	D	D	slurry impoundment, gw @ 16m
Martin County, KY - B	441	396	-10	C	C	slurry impoundment, gw @ 44m
Martin County, KY - C	441	428	-3	C	C	slurry impoundment, gw @ 44m
Martin County, KY - D	370	345	-7	C	D	slurry impoundment, gw @ 35m
Orange, CA - A	347	370	7	D	C	
Orange, CA - B	422	413	-2	C	C	
Las Vegas, NV - A	484 ²	507	5	C	C	
Las Vegas, NV - B	1048 ²	1096	5	B	B	
Las Vegas, NV - D	818 ²	846	3	B	B	
Las Vegas, NV - C	906 ²	948	5	B	B	
San Francisco, CA - A	716 ²	831	16	C	B	shallow sed. rock
San Francisco, CA - B	626 ²	565	-10	C	C	shallow sed. rock
Terminal Island, CA	196 ²	203	3	D	D	gw @ 5m
Terminal Island, CA	185 ³	203	10	D	D	same as above

1. Actual V_{s30} from modeled SASW data unless otherwise noted.
2. V_{s30} from modeled combined SASW and refraction microtremor data
3. V_{s30} from PS suspension logging data

The 53 surface wave soundings presented above were acquired on 20 different projects. One project also included a PS suspension log for a 54th comparison. Twenty-one of the soundings were acquired in Southern California, 15 in Northern California, 4 in Nevada, 4 in Colorado, 4 in Kentucky and 5 on Sakhalin Island, Russia. The average and median error/difference between the predicted and actual V_{s30} are 6 and 5%, respectively. Of the 54 comparisons between predicted and actual V_{s30}, 7 have differences

of 10% and 6 have differences of above 10%. Of these 13 soundings, 6 were acquired at sites with shallow bedrock and the associated abrupt increase in velocity. An additional 4 of the soundings were at Class D sites with V_{s30} differences of 18 to 38 m/s. Only 3 of the 54 comparisons were assigned different site classes based on actual versus predicted V_{s30} . The above comparison confirms previous estimates that the predictive regression relationship between V_{s30} and V_{R40} is generally reliable to within 10%. Further testing, particularly at sites outside California would still be beneficial.

DISCUSSION AND CONCLUSIONS

A large body of work has developed in support of using surface wave methods for accurate estimation of V_{s30} . Demonstrated reliability and accuracy recommends this method for standard practice. The variety of applications and techniques available allow broader application in a variety of circumstances, including urban settings where boreholes are prohibitive. We continue to observe that the results from surface wave methods probably represent the average properties of the entire site better than a single borehole measurement, because surface wave measurements are averaged over a larger volume of the subsurface.

A simple method of estimating V_{s30} from V_{R40} was previously been presented (Brown et al., 2000a, 2000b) and is discussed again, herein. Recent experience with this method confirms previous estimates that it is generally reliable to within 10%. This method can be adapted to any surface wave technique including the SASW, MASW, array microtremor and refraction microtremor methods and offers a very efficient and cost effective means to determine V_{s30} on a large scale.

The V_{s30} method is not designed to replace complete forward or inverse modeling of surface wave dispersion data, rather it offers a means for rapid, cost effective characterization of large areas such as in seismic hazard zonation studies and for determining V_{s30} for UBC/IBC site classification. We believe that the simplified V_{s30} method using SASW, MASW or microtremor data can reliably be used for site classification providing V_{s30} is not within 10% of a site class boundary. If the predicted V_{s30} is between 5 and 10% of a site class boundary then full modeling of surface wave data should be implemented to determine V_{s30} . If V_{s30} is within 5% of a site class boundary, confirmation using borehole velocity techniques could be considered depending on the nature of the structure being constructed and local seismic hazard. Borehole velocity measurements may only provide better V_{s30} estimates than surface wave techniques when data quality is high and the V_s of subsurface soils does not exhibit significant lateral variation. However, corroboration between two methods at sites with V_{s30} near a class boundary provides an increased level of confidence. Of course, when high resolution data on the vertical variation of V_s with depth is required; borehole techniques, particularly PS suspension logging and the crosshole seismic method are expected to provide superior results.

When conducting surface wave investigations at a single location for determining V_{s30} for site classification, it may be practical to acquire a complete set of sounding data even if the V_{s30} method is used to analyze the data. A complete surface wave dispersion curve would then be available for forward/inverse modeling if predicted V_{s30} is within 10% of a class boundary. Depending upon field procedures, it may only take an extra hour or two to acquire a complete set of surface wave dispersion data - four or five additional receiver spacings when using SASW, smaller receiver spacing dataset when using MASW or a shallow MASW/SASW sounding to define near-surface velocity structure when using the microtremor method.

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